This report describes and documents LossCalc, Moody’s model for predicting loss given default (LGD): the equivalent of \((1 - \text{recovery rate})\). LGD is of natural interest to investors and lenders wishing to estimate future credit losses. LossCalc is a robust and validated model of United States LGD for bonds, loans, and preferred stock. It produces estimates of LGD for defaults occurring immediately and for defaults occurring in one year. These two point-in-time estimates can be used to predict LGD over holding periods.

LossCalc is a statistical model that incorporates information on instrument, firm, industry, and economy to predict LGD. It improves upon traditional reliance on historical recovery averages. The model is based on over 1,800 observations of U.S. recovery values of defaulted loans, bonds, and preferred stock covering the last two decades. This dataset includes over 900 defaulted public and private firms in all industries.

We believe LossCalc is a meaningful addition to the practice of credit risk management and a step forward in answering the call for rigor that the BIS has outlined in their recently proposed Basel Capital Accord.

**Figure 1**

Recovery Experience and Forecasts for Senior Unsecured Bonds over Time

This figure shows the predicted average recoveries over time of LossCalc (thick red line) versus the long-term average as it evolves over time (thin line). The bars show the actual recovery for each year. Dark colored bars indicate years with smaller sample size.
We have organized the remainder of this report as follows:

Section 1, Loss Given Default: discusses the importance and difficulty of estimating loss given default (LGD), which is of natural interest to investors and lenders. Its estimation is as important as the probability of default in predicating credit losses.

Section 2, The LossCalc Model: describes the LossCalc LGD model and summarizes the factors of the model, the modeling framework, model validation results, and the dataset. We discuss each of these topics in more detail in subsequent sections.

Section 3, Factors: describes the nine predictive factors that drive the estimate of LGD in the LossCalc model.

Section 4, Framework: describes the modeling approach we used to develop LossCalc.

Section 5, Validation and Testing: documents the performance of the model in out-of-sample, out-of-time testing, which we find to be superior to traditional LGD estimation methods.

Section 6, The Dataset: describes the data used to develop the model and gives details of the dataset which contains over 1,800 observations of U.S. recovery values of defaulted loans, bonds, and preferred stock covering the last two decades.

Highlights

1. We describe Moody’s LossCalc™, a predictive statistical model of loss given default (LGD), the factors in the model, the modeling approach, and the accuracy of the model.

2. We find that LossCalc performs better at predicting LGD than traditional historical average methods. LossCalc:
   • exhibits lower prediction error and higher correlation with actual losses;
   • is more powerful at predicting low recoveries; and
   • produces narrower confidence bounds.

3. LossCalc produces estimates of LGD for defaults occurring immediately and for defaults occurring in one year.

4. Moody’s has based LossCalc on over 1,800 observations of U.S. recovery values of defaulted loans, bonds, and preferred stock covering the last two decades. This dataset includes over 900 defaulted public and private firms in all industries.

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1. LOSS GIVEN DEFAULT

Loss Given Default, the equivalent of \( 1 - \text{recovery rate} \) is of natural interest to investors and lenders who wish to estimate potential credit losses. However, it is inherently difficult to predict what the value or cash flows of an obligation might be if it became defaulted. When a loan is made or a security purchased, the holder does not normally think it likely that the obligor will default. Yet, to predict LGD, the creditor must imagine the circumstances that would cause default and the condition of the obligor after such default.

The practicalities of the U.S. bankruptcy process make it difficult to predict how the value of a bankrupt firm will be apportioned among its creditors. In U.S. bankruptcy legislation, the guiding principal for allocating a firm’s liquidation value amongst its creditors is the seniority hierarchy or “classes” of claims applied using the Absolute Priority Rule. In its strictest interpretation, each class has a relative ranking. Funds available for distributions are paid first to the highest-ranking class until the firm’s obligations to it are fully satisfied. Only then would the next highest-ranking class start to be paid.

This strict interpretation of priority is almost never fully adhered to (see for example Longhofer & Carlstrom [1995]). Indeed, bankruptcy procedures include the drafting of a “plan” that can only proceed speedily upon the approval of multiple levels of claimants. Thus, to gain control of the company quickly, and stop any further deterioration of asset values from occurring, there is incentive for senior claimants to make concessions to junior claimants. In the end, recovery rates have a lot to do with not only the assets of the bankrupt firm and the seniority of a petitioner’s claim, but also the relative strength of negotiating positions.

LGD is as important as the probability of default in estimating potential credit losses. We can see this immediately by considering the formula for credit loss:

\[
\text{Potential Credit Loss} = \text{Probability of Default} \times \text{Loss Given Default}
\]

A proportional error in either the probability of default or LGD affects potential credit losses identically. Yet, much more resource and effort is employed to estimate probability of default. Many different modeling techniques are applied to default probability; from statistical methods based on accounting data to structural (Merton) models to hybrids such as Moody’s RiskCalc™.

In sharp contrast, LGD is typically estimated by appealing to historical averages, usually segregated by debt type (loans, bonds and preferred stock) and seniority (secured, senior unsecured, subordinate, etc.). Figure 2 displays detailed historical information on recoveries.

![Figure 2](image)

**Figure 2**

Default Recovery by Debt Type and Seniority, 1981-2000

This figure is adapted from Moody’s 2001 annual default study; see Exhibit #20 in Hamilton, Gupton & Berthault [2001]. It highlights the wide variability of recoveries even within individual seniority classes. The shaded boxes cover the inter-quartile range with the median marked as a white horizontal line. Squared brackets cover the data range except for outliers that are marked as horizontal lines.
The extreme range of the historical data should make one wonder about its use. For example, suppose one used the median (32%) to estimate recovery on a senior subordinated bond. The median absolute error of that estimate (out of sample) is over 22%. Compared to the 32% median, the range of the error is almost 70% (=22/32) of the estimate. The same percentage absolute error in default probabilities for a senior subordinated bond with a senior implied rating of Baa and a 10-year maturity would imply a historical default rate somewhere in the very wide range of Aa-to-almost-Ba!

Recently, regulatory bodies have focused more closely on LGD analysis. The proposed New Basel Capital Accord (Basel, 2001) addresses the issue explicitly:

Where there is no explicit maturity dimension in the foundation approach, corporate exposures will receive a risk weight that depends on the probability of default (PD) and loss given default (LGD).

(Basel, § 173)

Banks would have the option of using conservative pre-defined LGD measures under the so-called foundation approach, but if they wish to qualify for the advanced approach:

...A bank must estimate an LGD for each of its internal LGD grades...Each estimate of LGD must be grounded in historical experience and empirical evidence. At the same time, these estimates must be forward looking...LGD estimates that are based purely on subjective or judgmental consideration and not grounded in historical experience and data will be rejected by supervisors.

(Basel, § 336 & 337)

We believe that LossCalc is a meaningful addition to the practice of credit risk management and a step forward in answering the call for rigor that the BIS has outlined in their recently proposed Basel Capital Accord.

2. THE LOSSCALC LGD MODEL

2.1 Overview

LossCalc is a robust and validated model of United States LGD for bonds, loans, and preferred stock. It produces estimates of LGD for defaults occurring immediately and for defaults occurring in one year.

The issue of prediction horizon has received little attention in previous recovery research, perhaps due to the static nature of a typical table of long-term historical averages. Applications of historical average tables typically use the same estimate of recovery irrespective of the horizon over which default might occur. This means that important considerations are ignored such as the point in the credit cycle or the sensitivity of a borrower to the economic environment. It is the nature of historical average LGD methods to be updated infrequently. In addition, new data will have a relatively small impact on longer-term averages.

In contrast, LossCalc is dynamic and able to give a more exact specification of LGD horizon that incorporates cyclic and firm specific effects. LossCalc’s immediate and one-year horizon forecasts would naturally fit different investor and risk management applications.

LossCalc incorporates information on instrument, firm, industry, and economy to predict LGD. It improves upon traditional reliance on historical recovery averages. We have developed the model on over 1,800 observations of U.S. recovery values of defaulted loans, bonds, and preferred stock covering the last two decades. This dataset includes over 900 defaulted public and private firms in all industries.

1. The 10-year default rate on a Baa is just under 8% (here we round from the historical 7.92% rate). Using the mean absolute deviation as a measure of error, we observed about a 22/32 = 70% error rate on the LGD estimate. The equivalent 70% difference in default probability would imply:
   - a lower bound of 8% - 0.7*8% = 2.4%; and
   - an upper bound of 8% + 0.7*8% = 13.6%.

   The Aa 10-year default rate is 3.1%, which is still higher than our lower bound, so the upper bound would be equivalent to at least a Aa-rating. The upper bound is below the 10-year Baa default rate of 7.92% and above the 10-year Ba default rate of 19.05%. Refer to Exhibit #30 and #31 in Keenan, Hamilton & Berthault (2000) for the default rates. This is a stylized example.
2.2 Time Horizon

The time horizon of LGD projections is an important aspect of credit risk that has unfortunately been absent from risk management practices. The valuation of a defaulted debt is far from static and should change with different forecast horizons. This is true for the valuation of any asset. Investors and lenders should match the tenor of the LGD projection to their exposure horizon.

Nevertheless, the prevailing practice is to treat LGD as static over the holding period. LossCalc projects LGD for two points in time: immediate and at one year. Assuming no knowledge of the individual obligor, the average time of a possible default would be about half way into the exposure period. This means that LossCalc’s immediate prediction of LGD should be applied to exposures maturing in less than one year and with an average time to default of less than six-months. The immediate version can also be used for debts that are already in default, particularly if market prices are not available.

The one-year version of LossCalc projects LGD for default in one year. Therefore, it is ideal for two-year exposures that have an average time to default of one year. The one-year LossCalc LGD is also the best prediction for exposures one year and greater. The user should note changes in exposure amount when determining which LGD projection to use.

2.3 Factors

As a proxy for the ultimate recovery on a defaulted instrument, we use the market value of defaulted debt one-month after default.

LossCalc uses nine explanatory factors to predict LGD. We have summarized these nine factors into four broad groups as shown below:

- **debt-type**: (i.e., loan, bond, and preferred stock) and **seniority grade**: (e.g., secured, senior unsecured, subordinate, etc.);
- **firm specific capital structure**: leverage and seniority standing;
- **industry**: moving average of industry recoveries; banking industry indicator;
- **macroeconomic**: one-year median RiscCalc default probability; Moody’s Bankrupt Bond Index; trailing 12-month speculative grade default rate; changes in the index of Leading Economic Indicators.

These factors have little intercorrelation, each is statistically significant, and together they make a more accurate prediction of LGD.

2.4 Framework

We have based LossCalc on a methodological framework similar to that used in Moody’s RiskCalc probability of default models. The broad steps in this framework are transformation, modeling, and mapping.

**Transformation**: We transform raw data into “mini-models.” For example, we have found it useful to transform certain macro-economic variables into composite indices, rather than use the pure levels. As another example, we find it useful to use average historical LGD by debt type and seniority.

**Modeling**: Once we have transformed individual factors and converted them into mini-models, we aggregate these using regression techniques.

**Mapping**: We statistically map the model output to historical LGD.

Each of the three steps to this process relies on the application of standard statistical techniques. We outline the details of these in Section 4.
2.5 Validation

We find that LossCalc is a better predictor of LGD than the traditional methodologies of historical averages segmented by debt type and seniority. By "better," we mean that:

- LossCalc estimates have significantly lower error.
- LossCalc makes far fewer large errors. A reduction in very large errors is the principal driver of the overall reduction in error. For example, LossCalc has about 50% fewer errors larger than 30% of par value.
- LossCalc estimates have significantly more correlation with actual outcomes. This means they have better tracking of high and low recoveries.
- LossCalc provides better discrimination between instruments of the same type. For example, the model provides a much better ordering (best to worst recoveries) of bank loans than historical averages.
- Over 10% of the time, the reduction in error rate is greater than 12% of original par value.
- LossCalc, on average, has tighter confidence bounds than other approaches so there is more certainty of recovery prediction.

2.6 The Dataset

We developed the model on over 1,800 observations of U.S. LGD of defaulted loans, bonds, and preferred stock covering the last two decades. This dataset includes over 900 defaulted public and private firms in all industries. The issue sizes range from $680 thousand to $2.0 billion, with a median size of about $100 million. The median firm size (assets at annual report before default) was $660 million, but ranged from $5.0 million to $37.7 billion. Neither debt size nor firm size appears significantly predictive of recovery rate in this dataset.

3. FACTORS

In this section, we describe the LGD variable and the explanatory factors of the immediate and one-year LossCalc models. The modeling framework is a statistical modeling approach. The central goal is to increase predictive power through the inclusion of multiple factors, each designed to capture specific aspects of LGD determination.

3.1 Definition Of Loss Given Default

We define recovery on a defaulted instrument as its market value approximately one-month after default. Importantly, we use security-specific bid-side market quotes. These prices are not "matrix" prices, which are broker-created tables specified across maturity, credit grade, and instrument type, without consideration of the specific issuer.

Moody's chose to use price observations one month after default for three reasons:

- it gives the market sufficient time to assimilate new post-default corporate information;
- it is not so long after default that market quotes become too thin for reliance;
- the period best aligns with the goal of many investors to trade out of newly defaulted debt.

This definition of recovery value avoids the practical difficulties associated with determining the post-default cash flows of a defaulted debt or the value of instruments provided in replacement of the defaulted debt. The very long resolution times in a typical bankruptcy proceeding compounds these problems.

Figure 3 shows the timing of price observation of recovery estimates and the ultimate resolution of the claims. Broker quotes on defaulted debt provide a far more timely recovery valuation relative to waiting to observe the completion of court ordered resolution payments. Market quotes are commonly available in the period 15-to-60 days after default. However, if no pricing was available or if we felt that a price was not reliably stated, then it did not enter our dataset.

---

2. This date is not always well defined. As an example, bank loan covenants are commonly written with terms that are more sensitive to credit distress than those of bond debentures. Thus, different debt obligations of a single defaulted firm may officially default on different dates. The vast majority of securities in our dataset are quoted within the range of 15-to-60 days of the date assigned to initial default of the firm's public debt. Our study found no distinction in the quality or explicability of default prices across this 45-day range.

Although it is beyond the scope of this report, there have been several studies of the market’s ability to price defaulted debt efficiently. These studies do not always show statistically significant results, but they consistently support the market’s efficient pricing of ultimate recoveries. At different times, Moody’s has studied recovery estimates derived from both bid-side market quotes and discounted estimates of resolution value. Both methods have their advantages and disadvantages. We find, consistent with outside academic research, that these two tend to be unbiased estimates of each other.

**3.2 Factor Descriptions**

Over the course of model development, we considered the inclusion of a number of predictive variables. We included factors only if they have both a strong economic rationale and statistical significance.

In all, the LossCalc models use nine factors to predict immediate LGD and a subset of eight factors to predict one-year LGD. We grouped the factors into four categories as shown in Table 1 below. The table highlights the four broad categories of predictive information: debt type and seniority, firm specific capital structure, industry, and macro economic. These factors have little intercorrelation and together make a significant and more accurate prediction of LGD. All factors enter both LossCalc forecast horizons (i.e., immediate and one-year) with the single exception of the U.S. speculative-grade default rate. We chose to have this indicator enter only the immediate model.

**Table 1: Explanatory Factors in the LossCalc Models**

<table>
<thead>
<tr>
<th>Category</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Debt Type and Seniority</td>
<td>Historical average LGD by debt-type (loan, bond, and preferred stock) and seniority (secured, senior unsecured, subordinate, etc.).</td>
</tr>
<tr>
<td>Firm-Specific Capital Structure</td>
<td>Seniority standing of debt in the firm’s overall capital structure; this is the relative seniority of a claim. Note that this is different from the absolute seniority stated in Debt Type and Seniority above. The most senior obligation of a firm might be, for example, a subordinate note.</td>
</tr>
<tr>
<td>Industry</td>
<td>Moving average of normalized industry recoveries. We have here controlled for seniority class.</td>
</tr>
<tr>
<td></td>
<td>Banking industry indicator</td>
</tr>
</tbody>
</table>

---

5. Note that we also considered factors that were not included in the model due to either lower power than competing alternatives or data sufficiency issues. They are not discussed here in detail. Some of these were: yields and spreads (e.g., BBB - AAA, Govt1, 2...10y, etc.), other macro factors (e.g., CPI, etc.), other financial ratios (e.g., EBIT / Sales, Current Liabilities / Current Assets, etc.), other instrument specific information (e.g., coupon, spread, etc.), and so forth.
3.2.1 Debt Type and Seniority

Historical average recovery rates, broken-out by debt type (loan, bond, preferred stock) and seniority (secured, senior unsecured, subordinate, etc.) are the starting points for LossCalc. Although historical averages are important, they account for less than half of the influence in predicting levels of recoveries in LossCalc, as shown in Figure 4.

Inclusion of historical averages does two things. First, it addresses the effects of the Absolute Priority Rule of default resolution. Second, it helps ensure that, on average, LossCalc will perform no worse than the prevailing practice of referring to long-term historical averages.

The relative seniority of debt (i.e., the debt’s rank within the capital structure of the firm) can be important to predicting LGD. For example, preferred stock is the lowest seniority class in a typical capital structure, but it might hold the highest seniority rank within a particular firm that has no funding from loans or bonds in its capital structure. In addition, in cases where a firm issues debt sequentially in order of seniority, it may happen that senior debt matures earlier leaving junior debt outstanding.

We designed LossCalc to consider a debt’s seniority in absolute terms, via historical averages, and in relative terms, when such data are available, within a particular firm. Both are predictive of LGD and are reasonably uncorrelated with one another. The relationship is well documented and straightforward. Each seniority class must compete with other classes for available funds.

It is reasonable to ask why we did not use a predictor such as “the dollar amount of debt that stands more senior” or “the proportion of total liabilities that is more senior?” While these seem intuitively more appealing, there are two main reasons we chose the simpler indicator:

Resolution Procedure: In bankruptcy proceedings, a junior claimant’s ability to extract concessions from more senior claimants is not directly proportional to his claim size. Junior claimants can force the full due process of a court hearing and so have a practical veto power on the speediness of an agreed settlement.
Availability of Data: Claim amounts at the time of default are not the same as original issuance/borrowing amounts. In many cases, obligations are paid down in part before the full maturity of the debt. Sinking funds (for bonds) and amortization schedules (for loans) are examples of this. Determining the exposure at default for many obligations can be challenging, particularly for firms that pursue multiple funding channels. In many cases, this data is unavailable. Requiring such an extensive detailing of claims before being able to make any LGD forecast would be onerous from both a modeling and usage perspective.

3.2.2 Firm Specific Capital Structure: Leverage

Intuitively, the capital structure of a firm is relevant to the funds available (in default) for the satisfaction of creditor claims. Said another way, the assets to liabilities ratio acts like a coverage ratio of the funds available versus the claims to be paid. A higher ratio of assets to liabilities is better.

However, leverage does not contribute to the prediction of LGD for secured credits. Such claims would look first to the value of their specific security and only secondarily seek satisfaction from the general funds of the defaulted firm.

3.2.3 Industry

Researchers frequently propose industry level segregation of recovery levels as being useful in recovery modeling. The idea is that an industry might consistently enjoy high recoveries or perhaps suffer recoveries that are consistently low across time. Our test of this was to compile average industry recovery levels across time and test the statistical significance in the average’s deviation from the overall average recovery.

We found this to work well for recoveries of bank defaults, which are consistently low across time. The rationale for modeling the banking industry by an indicator variable is as follows:

Seniority of Deposits over Public Debt: Deposits are commonly the majority of obligations of a bank and they enjoy a "super-seniority" position relative to public debt in bankruptcy.

Liquidity of Banks: Unlike the plant and equipment found in other industries, the financial assets and liabilities of a bank are typically very short in duration and liquid. In response to this short-term nature (and to help stem systemic liquidity crisis), the Federal Reserve offers access to liquidity via the Fed’s Discount Window. Thus, it is difficult for creditors to "force" liquidity default on a bank that still has many good quality assets available to pay off its liabilities. Consequently, by the time banks default it is sometimes too late, when most of the good assets are insufficient.

Fed Forbearance: Historically, bank regulators have allowed insolvent banks to remain open. During the time that regulators allow insolvent banks to remain open, banks use up their assets to pay off short-term liabilities and the available asset coverage for long-term creditors falls proportionately.

However, we also found strong evidence of industry specific ebbs and flows in the recovery rates that differed in time between industries. We found that some industries would enjoy periods of prolonged superior recoveries, but fall well below average recoveries at other times. A simple industry bump-up or notch-down, held constant over time, does not capture this behavior. To address this, we grouped firms into twelve broad industries and created moving averages of recoveries.

3.2.4 Macro Economic

The intuition behind the inclusion of macro economic variables is that defaulted debt prices tend to rise and fall together as a population rather than being fully independent of one other. Another way of saying this is that recoveries have positive and significant intercorrelation within bands of time. This type of correlation has potentially material implications for portfolio calculations of Credit Value-at-Risk. The leading vendor models of Cr-VaR implicitly set this correlation to zero and would thus understate Cr-VaR in this regard.

6. We tested this on a sub-population selected to have fully populated claim amount records. The best predictor of recoveries, both univariately and in combination with a core set of LossCalc regressors was a simple flag of standing the highest. As alternatives, we tested dollars (and log of dollars) of superior claims and proportions of superior claims.


3.2.4.1 One-Year RiskCalc Probability of Default

Moody’s RiskCalc for Public companies can measure changes in the credit quality of corporate obligors with publicly traded equity. RiskCalc is a hybrid model that combines two credit risk modeling approaches: (a) a structural model based on Merton’s options-theoretic view of firms; and (b) a statistical model determined through empirical analysis of historical accounting data. LossCalc uses time series of median RiskCalc PDs.

3.2.4.2 Moody’s Bankrupt Bond Index

LossCalc uses Moody’s Bankrupt Bond Index (MBBI), a monthly price index measuring the return of a broad cross-section of long-term public debt issues of corporations that are currently in bankruptcy. The bonds of defaulted or distressed companies that have not yet filed for bankruptcy are not included in the index. MBBI includes both Moody’s-rated and non-rated debt from U.S. and non-U.S. obligors, denominated in U.S. dollars.9

3.2.4.3 Trailing 12-month Speculative Grade Average Default Rates

While RiskCalc provides a measure of the outlook for default rates, we also found it useful to include a measure of historical default rate behavior. We capture this through the inclusion of the trailing 12-month speculative grade default rate for Moody’s rated firms. This factor did not exhibit strong predictive power for the one-year model and is thus included only in the immediate model where it was strongly significant.

3.2.4.4 Changes in Index of Leading Economic Indicators

We found that the change in Gross Domestic Product computed over the upcoming duration of default resolution was strongly predictive of recoveries. Of course, this future information could never be available for prediction. Nonetheless, this relationship indicates something of the process underlying recoveries.

As a proxy, we chose a readily accessible series that seeks to address this same information, the Index of Leading Economic Indicators.10 While its correlation with recoveries, as shown in Figure 5, is far from perfect, it is reasonable and carries significant predictive power. There is visible correlation between it and a time-series of aggregated recovery experience.

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9. The MBBI historical series was revised in January 2000. Refer to “The Investment Performance of Bankrupt Corporate Debt Obligations”, February 2000, Moody’s Special Comment for details on this revision and about the construction of the MBBI.

10. The Conference Board, Inc. produces the Leading Economic Indicators. See their site at http://www.globalindicators.org, for details.
4. FRAMEWORK

In this section, we provide detail regarding the steps of the LossCalc modeling process.

We have based LossCalc on a methodological framework similar to Moody’s RiskCalc default probability models. The steps in this framework are transformation, modeling, and mapping.

Transformation: We transform factors into “mini-models.” For example, we find it yields better prediction to transform certain macro-economic variables into composite indices, rather than using the pure levels. As another example, we find it yields better prediction to use average historical LGD by debt type and seniority.

Modeling: We aggregate mini-models using regression techniques.

Mapping: We map model output to historical LGD statistically.

4.1 Establishing A Dependent Variable

The defaulted debt prices that we use to project LGD are not normally distribution. An alternative distribution that better approximates the prices in our data is the Beta-distribution, shown in Figure 6. This figure shows the actual distribution of recoveries and a Beta-distribution fit to approximate it. The highly asymmetric nature of the distribution is evident in both the empirical and fit distributions.

The Beta-distribution ranges between zero and one, but is not restricted to being symmetrical. It can be specified by two parameters loosely referred to as its “center” (α) and “shape” (β). This means that it has great flexibility to describe a wide variety of distributions, such as those with high probabilities “massed” on the upper or lower limits of zero or one. These mathematical properties closely align to, and are very useful in describing, ratio values such as “recovery rates.”11

11. Because there are a small, but non-trivial, number of instances where the market prices of defaulted bonds are greater than par, we add a third parameter to the usual zero-to-one interval to describe our Beta distributions: the maximum value for the interval.
In our dataset, the distribution of bond recoveries shows a characteristic left-side peak and right-side skew. Figure 7, below, compares a Beta-distribution with the corresponding Gaussian (Normal) for the same mean and SD. It is often more convenient to work with symmetrical distributions, such as the Normal, than with bounded and skewed ones, such as the Beta. Fortunately, the mathematical transformation between the two is straightforward.

We first group obligations according to debt-type (i.e., loans, bonds, and preferred stock) since these broad categories exhibit markedly different average recovery distributions. We then transform the variables from Beta to Normal space. Conveniently, this only requires a) the mean, \( \mu \), and the standard deviation, \( \sigma \), of the observed recoveries and b) the bounding values. Appendix A gives details of this parameterization and transformation. The result is a normally distributed variable with the same probability as the equivalent raw recovery had in Beta-space.

---

12. We expect that the particular values that we find for each debt-type’s \( m \) and \( s \) (and so the parameter values that we assign to the a’s and b’s) will change from time to time as we update LossCalc with additional data.
4.2 Transformation And Mini-modeling

We gained a great deal of insight by assessing predictive factors on a stand-alone (univariate) basis. We transform some of the input factors to make them better stand-alone predictors before assembling an “overall” model. If these transformations create a truly significant factor, then we typically rename its transformation a "mini-model.”

In LossCalc for example, both the Seniority-Class variable and the Industry LGD variable are “mini-models.” Each is indicative on a stand-alone basis as a measure of recovery values. Other instances of mini-modeling were less dramatic, such as a leverage ratio, logs, or changes versus levels in a time-series, etc. Two other model components are useful to note.

4.2.1 The Index of Macro Changes

LossCalc uses an index calculated by statistically weighting the changes in levels of various macro economic indicators into a composite index, which is in effect an estimate of the average recovery that would be implied by these macro changes only. We do this weighing as we step forward in time each month. This both maximizes its overall predictive power and minimizes month-to-month changes in the weighting.

4.2.2 Factor Inclusion by Seniority Class and Industry

The model drops certain factors in certain cases. For example, although leverage is one of the nine predictive factors in the LossCalc model, it is not included in the case of financial institutions. These are typically highly leveraged with lending and investment portfolios having very different implications than an industrial firm’s plant and equipment.

Similarly, we do not consider leverage when assessing secured debt. The recovery value of a secured obligation depends primarily on the value of its collateral rather than the netted value of general corporate assets.

4.3 Modeling And Mapping: Explanation To Prediction

The modeling phase of the LossCalc methodology involves statistically determining the appropriate weights to use in combining the transformed variables and mini-models described in the previous section. The combination of all the above predictive factors is a linear weighted sum, derived using regression techniques. The model takes the additive form:

\[
\hat{r} = \alpha + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \ldots + \beta_kx_k
\]

Where the \(x_i\) are the transformed values and mini-models described above, the \(\beta\), are the weights and is the normalized \(r\) is the recovery. Note that at this point \(r\) is stated in “normalized space” and still needs to be transformed back into “dollar space.” So the final step is to apply the inverse of the Beta-distribution transformation (discussed above) to the three cases of loans, bonds, and preferred stock. See Appendix A for more details.

4.4 Confidence Interval Estimation

LossCalc also provides an estimate of the confidence interval (i.e., upper and lower bounds) on the recovery prediction. Confidence intervals (CI) provide a range around the prediction within which we anticipate the actual value to fall a specified percentage of the time. The width of a confidence interval provides information about the precision of the estimate. For example, we do not typically find that the actual value exactly matches the prediction every time. How far off might it be?

An 80% confidence interval around a predicted value is the range (bounded by an upper bound and lower bound) in which we are confident the true value will fall 80% of the time. Therefore, we would only expect the actual future value to be below the lower bound or above the upper bound, 20% of the time.

Confidence intervals have received surprisingly little attention in the recovery literature. Many investors are surprised to learn of the relatively high variability around the estimates of recovery rates produced by tables, illustrated in Figure 2.

13. Note that this is similar in some ways to the creation of univariate default curves used in the RiskCalc models. In this case, the transformation involves a multivariate representation. (See, for example, Falkenstein & Boral [2000]).
Although regression models produce a natural estimate of the (in-sample) confidence intervals, we found these relatively wide. We developed, estimated, and validated a conditional CI prediction approach that produced narrower ranges of confidence. In effect, a multi-dimensional lookup table results in narrower confidence intervals. The table has dimensions for debt type and seniority as well as others such as macroeconomic factors, etc. Each cell in the table contains information on the distribution of prediction errors for LossCalc. By using this table, we can calculate empirical upper and lower bounds of a confidence interval. This methodology was tested out of sample and produced robust results, as discussed in Section 5.

5. VALIDATION AND TESTING

The primary goals of validation and testing are to:

- determine how well a model performs;
- ensure that a model has not been overfit and that its performance is reliable and well understood;
- confirm that the modeling approach, not just an individual model, is robust through time and credit cycles.

To validate the performance of LossCalc, we have used the approach adopted and refined by Moody’s and used to validate RiskCalc, Moody’s default prediction models. The methodology we use, termed walk forward validation, involves fitting a model on one set of data from one time period and testing it on a subsequent period. We then repeat this process, moving through time until we have tested the model on all periods up to the present. Thus, we never use data to test the model that we used to fit its parameters and so we avoid over-fitting. We can also assess the behavior of the modeling approach over various economic cycles. Walk forward testing is a robust methodology that accomplishes the three goals set out above.

Model validation is an essential step to credit model development. We must take care to perform tests in a rigorous and robust manner while also guarding against unintended errors. For example, it is important to compare all models on the same data. We have found that the same model may get different performance results on different datasets, even when there is no specific selection bias in choosing the data. To facilitate comparison, and avoid misleading results, we use the same dataset to evaluate LossCalc and competing models.

Sobehart, Keenan, & Stein [2000] describe the walk-forward methodology more fully. Appendix B of this document gives a brief overview of the approach.

5.1 Alternative Recovery Models Used As Benchmarks

The standard practice in the market is to estimate LGD by some historical average. There are many variations in the details of how these averages are constructed: long-term versus moving window, by seniority class versus overall, dollar weighted versus simple (event) weighted. We chose two of these methodologies as being both representative and broadly applied. We then use these traditional approaches as benchmarks against which to measure the performance of the LossCalc models.

5.1.1 Table of Historical Averages

As noted, the dominant paradigm for LGD estimation is historical averages. It is important to realize that the published research on recovery (e.g., Moody’s annual default studied) typically presents statistics for an aggregated period. Thus, these type of reports cannot be used for walk forward testing since they include information that is often only available after a particular instrument defaulted. For example, Moody’s studies, completed in 1996, 1998, 1999, and 2000 would contain future information for much of the testing period.

We wanted to emulate the prevailing use of these tables — updating them, as one would step one year forward in time each year. Said another way, analysts understanding of the long-term historical recovery average evolves with each year’s new information. We tabulated these averages, for each debt-type, seniority grade, and year in our sample. This procedure replicates the common practice of LGD estimation and, with Moody’s sizable dataset, it represents a high quality implementation of this "classic lookup" approach.
5.1.2 The Historical Mean Recovery Rate

We have also observed that many market participants use a simple historical average recovery rate as a recovery estimate. To emulate this measure, we recalculate the average historical recovery rate each year as well.

5.2 The LossCalc Validation Tests

Validation testing for LossCalc is somewhat different from the testing procedure implemented for RiskCalc. This is because LossCalc produces an estimate of an amount (of recoveries) rather than some likelihood (of default). Therefore, LossCalc seeks to fit a continuous variable as opposed to predicting the binary outcome of default/no default. Thus, the diagnostics we use to evaluate its performance reflect this.

There are two important measures of the model. The first is accuracy: how well does the model predict actual losses experienced by an investor or lender? The second is efficiency: how wide are the confidence intervals on predictions? In general, these are related. Narrower confidence intervals typically (not always) arise from better prediction. Narrower confidence intervals allow better estimation of expected losses, Value-at-Risk, and (potentially lower) economic capital requirements.

In the next several sub-sections, we present measures of the LossCalc model performance in both the immediate and one-year cases. We compare LossCalc against both historical average approaches.

Since 1991 was the first year that we had enough data to build a sufficiently reliable model, unless otherwise stated, we used 1992 as the first out-of-sample year for which to predict. Following the walk-forward procedure, we constructed a validation result set containing over 850 observations, representing over 500 different firms from Moody’s extensive database in the years 1992 - 2001. This result dataset was just under half of the total observations in the full dataset. It was a representative sampling of rated and unrated public and private firms in all industries.

5.2.1 Prediction Error Rates

As a first measure of performance, we examined the error rate of the model. By convention, this is measured with an estimate of the mean squared error (MSE) of each model. The MSE is calculated as:

\[ MSE = \frac{\sum (r_i - \hat{r}_i)^2}{n - 1} \]

where \( r_i \) and \( \hat{r}_i \) are the actual and estimated recoveries, respectively, on security \( i \). The variable, \( n \), is the number of securities in the sample.

Models with lower MSE have smaller differences between the actual and predicted values and thus predict more closely the actual recovery.

We note that there is approximately the same improvement in performance (reduction in MSE) as one moves from the table of historical averages to LossCalc as there is when one moves from a simple historical average to a table.
The difference in error rates is not driven by a reduction in small errors but by the reduction in large errors. The median difference in error rates is relatively small (although significant). However, LossCalc has about 50% fewer errors larger than 30% of par value: the table of historical averages produces about 270 versus 185 for LossCalc in the test set (Table/LC ≈ 147%). Thus, in general, LossCalc, when it produces an error, tends not to produce as many very large ones.

It is sometimes useful to think in terms of the difference in error rates between two models as a type of “savings.” For example, over 10% of the time, the “savings” in absolute error rate is greater than 12% of par value. The median “savings” in error rate from using LossCalc is more modest, slightly under 3% of par value. This means that in half of the cases, the reduction in error was better than about 3%. For example, a table estimate of 30% loss might be more accurately described using LossCalc as having only a 27% loss, which would make approximately a 10% difference in the LGD estimate.

Importantly, there are some individual cases where LossCalc does not perform as well as a table of historical averages. However, the sum of these LossCalc errors is much lower than the sum of LossCalc’s savings when LossCalc outperforms the traditional table. In other words, for almost any cut-off, the benefit of using LossCalc outweighs the risks since the potential savings are greater than the potential cost. For example, less than one quarter of the time, in only the worst 25% of all cases, the table beats LossCalc by more than about 3%. In contrast, in the best 25% of cases LossCalc outperforms the traditional table.

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14. This is for the immediate model. The one-year model performed almost as well with 196 large errors to 270 for the table, or 37% fewer large errors.
15. Measured as \(|\text{Table Error} - |\text{LossCalc Error}|\)
the table by saving over 7% or more. The ratio of error savings/cost at each point is in the range of 1.5 times to about 2 times more savings than cost. Thus, LossCalc gives about 1.5 to 2 times more “savings” relative to error rate “cost.”

5.2.2 Correlation with Actual Recoveries

Next we examined the correlation of the various models’ predictions with the actual loss experience. In this case, models with higher correlation exhibit predictions that are high when actual recoveries are high and low when actual recoveries are low more often than those that have lower correlation with the actual losses observed for defaulted securities.

Figure 9, below, shows the correlation of predicted versus actual for the candidate models, also shown in tabular form in Table 3. Here we note the interesting finding that the historical average, out of sample, exhibits a negative correlation with actual experience. In other words, in general for years with higher than average recoveries, it predicts lower than average recoveries and vice versa. This may partially be a result of the relative lack of variability of the historical average (it changes value only once a year and is constant for all securities in that year). However the negative correlation here may simply be a result of the way a moving average is constructed as the economy moves through the business cycles. A moving average may be moving up due to last year’s economic boom just when it would do better to move down due to this year’s economic bust.

![Figure 9](image)

**Correlation of LossCalc Models and Alternatives with Actual Recoveries**

This figure shows the out-of-sample Correlation for LossCalc, the Table of Averages and the Historical Average. It is clear that over both the immediate and one year horizons, LossCalc has better correlation in comparison with the two alternatives.

### Table 3: Correlation of LGD Prediction Accuracy Across Models and Horizon

<table>
<thead>
<tr>
<th></th>
<th>Immediate</th>
<th>One Year</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Correlation</td>
<td>Bootstrap-SE</td>
</tr>
<tr>
<td>Historical Average</td>
<td>-0.13</td>
<td>0.024</td>
</tr>
<tr>
<td>Table of Averages</td>
<td>0.42</td>
<td>0.029</td>
</tr>
<tr>
<td>LossCalc</td>
<td>0.55</td>
<td>0.024</td>
</tr>
</tbody>
</table>

Listed here are the specific values illustrated in Figure 9 above.

In all cases, the bootstrap standard errors were on the order of 3 points of correlation, as shown in Table 3.
5.2.3 Relative Performance for Specific Debt Types

In Figure 10 we show the relative performance of LossCalc vs. the classic lookup table with respect to both MSE and correlation for bonds and loans, both of which have various levels of seniority associated with them and thus allow for differentiation within the debt type in the table.

![Figure 10](image_url)

This figure shows the relative increase in performance by debt type. By both MSE and correlation measures, LossCalc increases predictive performance dramatically. As a specific example, the improvement in correlation with the realized LGD between a table and LossCalc (at the one-year horizon) is shown in the bottom right chart. For example, by this measure, LossCalc is 370% better than a Table of Average LGD for bank loans.

By both MSE and correlation measures, LossCalc increases predictive performance significantly. While by both measures, the performance differential is obvious; it is worth discussing the rather dramatic increase in performance along the dimension of correlation. It is somewhat counter intuitive, since the increase in overall correlation is on the order of 50% while the increase in correlation within specific classes is on the order of 150% - 375%.

This can be understood in the context of how the two approaches to recovery prediction differ. The table’s main mechanism for predicting recoveries is segregation by debt type. After this segmentation, the only additional information the table uses is seniority. Taking senior subordinated bonds as an example, the out-of-sample correlation between the table’s predictions and the actual recoveries is only about 9%. (The correlation is not zero since the table is updated each year in the step forward testing and thus is not constant.) In contrast, for this same senior subordinated bond class, the LossCalc immediate model correlation is about 30%, or 3½ times as high.

Thus, the historical table focuses primarily on the between-group (debt type and seniority) variability rather than the within group instrument and firm specific variability in recoveries. In contrast, LossCalc’s use of additional information beyond two-way conditioning allows it to incorporate both within- and between-group variability more completely. Thus, the improvement in correlation is a reflection of the typically very low correlation of the table once we narrow the analysis down to the individual rows or cells in an historical table.

5.2.4 Prediction of Larger Than Expected Losses

By both the MSE and correlation measures, LossCalc out-performs the alternative approaches. However, in addition to concerns about accuracy, many investors and lenders are downside averse: they are most concerned about model error when losses are more severe than estimated. The final test of model predictive performance that we report here was motivated by this observation.
The test was designed to evaluate each model’s ability to predict cases in which actual losses were greater than historical expectations.

The test proceeded as follows:

1. Using the most recent information available up to the time of a default, we first labeled each record with respect to whether the actual loss experienced was greater or less than the historical mean loss for all instruments to date.
2. We then ordered all out-of-sample predictions for each model from largest predicted loss to smallest predicted loss.
3. Finally, we calculated the percentage of larger than average losses each model captured in its ordering using standard power tests.

This approach allowed us to convert the model performance to a binary measure which in turn allowed us to use familiar metrics and diagnostics such as power curves and power statistics to measure performance.

All things being equal, if a model was powerful at predicting larger than average losses, we would expect the largest loss predictions to be associated with the actual above average losses and the lowest loss predictions to be associated with below average losses. (On a power curve, this would result in the curve for a good model being bowed out towards the Northwestern corner of the chart. The random model would be a 45° line showing no difference in association between high and low ranked obligations.) While, this metric coarsens somewhat the actual model output, we have found that it provides a valuable perspective in evaluating recovery model performance.

The results of this analysis are shown in the panels of Figure 11. The figure shows both the Cumulative Accuracy Profile (CAP)16 at left and the area under the curves at right. The larger this area, the more accurate the model. In this case, for a perfect model, this area would be 1.0.

The figure shows that both the table and LossCalc models perform considerably better than random at differentiating high- and low-loss events, but that the LossCalc models outperform the table by a considerable margin.17 This relationship persists over both the immediate and one year horizons. The comparison of areas under the curves confirms this observation.

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16. As a technical note, the power curves shown here differ from the CAP plots we typically use to evaluate default models in that only the “goods” are shown on the x-axis. This is done to facilitate analysis since there are a large number of “bads” (below average) events. CAP plots and power curves measure the same quantities but present them in different ways. For a detailed discussion of CAP plots, refer to Sobehart, Keenan, & Stein [2000].

17. Note that tie breaking was not done in this case, so plateaus are still evident in the figures. A plateau indicates two (or more) instruments with the same model score. In principle, if one was a “bad” and the other was not, the ordering of these becomes important. These plateaus could be smoothed too so that the estimation was more accurate, although visual inspection suggests that the differences would not change the overall conclusions.
5.2.5 Reliability and Width of Confidence Intervals

To test the reliability of the confidence intervals produced by the models, we examined them along two dimensions: width and reliability. The average width of a confidence interval provides information about the precision and efficiency of the estimate. To the extent that confidence intervals of one model are narrower than confidence intervals for another model, then this implies that the former predictions are more reliable. From an economic perspective, it implies more certainty regarding the capital that might be required to protect against losses.

However, a CI can be made arbitrarily narrow if one ignores that the counter-balancing constraint is the reliability of a model’s CI at actually predicting the true interval. Said otherwise, if a given model produces an a% confidence interval, then in practice out-of-sample, we would expect to observe actual realized losses outside the interval about 1-a% of the time. To the extent that the model experienced an undue number of actual losses outside its "narrow" CI, this would provide evidence that the "narrow" CI were, in fact, too narrow.

To examine these two dimensions of the CI, we first generated CIs for each model and calibrated them to in-sample data. We report the average widths of these CI in the first (left) section of Figure 12. We then tested out-of-sample and out-of-time the number of cases in which the actual observed losses exceeded the predicted interval.

As we discuss below, we examined several methods for CI prediction. Some of these required the use of actual prediction errors from previous periods. Thus, this type of testing requires more data than accuracy testing. Therefore, we were more limited in the amount of data available for this validation. Nonetheless, we had a large number of recovery observations on which to draw. We chose the period prior to 1998 for estimating the CI and the subsequent period for out-of-sample-out-of-time testing. This resulted in about 500 observations for tests at the one-year horizon and close to 600 for the immediate tests.

Figure 12, shows that LossCalc’s CIs are more precise (narrower) than both the parametric (standard deviation) and quantile estimates from the table. However, uneven coverage percentages add some uncertainty to the analysis.

For example, for the immediate horizon version of LossCalc, the actual out-of-sample coverage of the historical table was higher than LossCalc signalling not only a more precise estimation, but also a more efficient one. However, the 1-year version shows a slightly higher out-of-sample coverage than the historical table indicating that the width of the CI could probably have been made tighter. Similarly, the width of the parametric CI for the table are likely optimistically narrow,
due to the higher than expected number of cases outside the CI. Unfortunately, there is no way to anticipate such variances from the expected CI a priori.

We can, however, ask the following question: What would the width of the CIs have been if all calculation approaches had the same out-of-sample coverage? This would give some insight into the relative width of these confidence bounds after controlling for coverage.

To address this, we adjusted the parameters of the confidence estimates to ensure that coverage of all methods on the out-of-sample data would be consistent with the LossCalc coverage. This then restricted the analysis to the evaluation of the comparative widths of the CI. We stress here that this adjustment would not be possible in practice since it relies on knowledge of the future for calibration of the parameters. We perform it here only to provide descriptive analysis of the the relative performance of the LossCalc CI. The results of this analysis are given in Figure 13. It is clear from the figures that the LossCalc estimates are narrower than other alternatives.

6. THE DATASET

The primary dataset for LossCalc is Moody's proprietary default and recovery database. This is the same default database that Moody's uses in its annual default study. In addition, this information was supplemented with other types of data such as financial statements and credit indices that allow for a more refined analysis.

We focus here on the secondary market pricing of defaulted debt as quoted one month after the date of default. Importantly, we use debt-issued specific market quotes. These prices are not “matrix” prices, which are broad broker-created tables keyed off maturity, credit grade, and instrument type with no particular consideration of the specific issuer.

6.1 Historical Time Period Analyzed

It is not clear that going back to the extreme limits of the historical record would produce the most useful model. This is because, as with any predictive model, experience that is more recent is likely to be closer in nature and of greater predictive power for the future.

Conversely, we have fewer recovery observations relative to Moody’s datasets used for RiskCalc to estimate the probability of default. Furthermore, we did not want the model to be overly influenced by any single default event, or even clusters.
of closely related defaults. This would argue that we should use as much data as possible, which would mean going back far in time.

Two considerations framed our selection of the historical period. First, we felt that the full specification and validation of our model could only be achieved satisfactorily if one or more (in the case of LossCalc, two) full economic cycles are included in the dataset. This criterion was motivated by our early studies, which found that the credit cycle was a strong determiner of recoveries. Second, our research also indicated that firm-level capital structure was also predictive of recovery levels. To tailor our recovery estimates to the details of specific firms, we deemed it highly desirable to have access to financial statement information.

For both of these reasons, the period we used was Jan-1981 to the present. This period covers two full credit cycles.

6.2 Scope Of Geographic Coverage And Legal Domain

Clearly, bankruptcy laws vary markedly across legal domains. UK law strongly seeks to protect creditors. French law does not recognize the priority of claims of specifically identified security. Some domains allow creditors to file a petition for insolvency. And this is just a sampling of the diversity of liquidation rules. Therefore, for this version of LossCalc, we have chosen to restrict the scope of the model to U.S. debt obligations only.

Having said this, as we move forward and fit future versions of LossCalc to other domains, we anticipate that many of our findings will hold.

6.3 Scope Of Firm Types And Instrument Categories

Seniority standing is especially important to this version of LossCalc because we are focusing exclusively on U.S. recoveries. American bankruptcy law applies the concept of the Absolute Priority Rule, which states that more senior claimants must be fully satisfied before more junior claimants can start to receive any of the defaulted firm’s liquidation/reorganization value. In practice, the actions in bankruptcy proceeding are more complicated, but this guiding principal makes debt’s seniority standing a leading component of recovery rate estimation.

Our dataset includes three broad debt instrument types: a) bank loans, b) public bonds, and c) preferred stock. Within loans, there are two seniority grades: "senior secured," which are the more numerous, and "senior unsecured." Public bonds subdivide into more seniority classes:
- senior secured;
- senior unsecured;
- senior subordinated;
- subordinated; and
- junior subordinated.

In addition to these five broad classes, we break out two specialized classes: corporate mortgages which are a kind of senior secured bond plus industrial revenue bonds (IRBs), which are a kind of senior unsecured bond.

Parenthetically, we make no distinction between the different types of preferred stock. In normal times, various factors make a real difference in the traded valuations of preferred stock. These include:
- fixed/floating rate payments;
- cumulative versus non-cumulative dividends; and
- convertibility.

None of these factors above is explicitly mentioned in the bankruptcy code. However, cumulative dividends may be a strong analogy with accrued interest for bonds, which are included in defaulted debt claims. As part of our continuing LGD research, we hope to assess whether bankruptcy courts act on this.

18. By definition, at the obligor level, the number of recovery observations is less than (or equal to) the number of default observations. There cannot be a recovery unless there has been a default observation. By comparison, RiskCalc has far more observations than LossCalc. However, a single default can also produce several instrument-level recovery observations if the obligor has multiple classes of debt outstanding.
19. See West & de Bodard [2000a,b,c] and Bartlett [1999].
As a final detail, we note that in the case of medium term note programs (MTNs), which are characterized by a large number of small issues, we consolidate the many individual issues into a single recovery observation per default event. The recovery rate realized for this proxy observation is the simple average of all the individual issuances. It happens that there was never large variability in the recovery estimates across issues within a single MTN program.

7. CONCLUSION

In this report, we described the research done to develop LossCalc, Moody’s loss given default (LGD) model. LossCalc is a multi-factor statistical model developed using a database of over 1800 defaulted instruments. It produces LGD estimates for bonds, syndicated loans, and preferred stock. LossCalc assesses information on four levels of analysis, including the characteristics of the instrument, the capital structure of the firm, and macro factors at both the economy and industry level.

The issue of prediction horizon for LGD is one that has not received much attention due to the largely static nature of the dominant historical average approach. This implicitly ignores the effects of the credit cycle and other time-varying environmental factors. LossCalc, by its dynamic nature, allows for a much more exact specification of LGD horizon and produces estimates on an immediate and one-year horizon.

We conducted extensive out-of-sample out-of-time validation of this model to determine how well it performed at predicting LGD compared to alternative approaches. The results of this benchmarking show that the model performs better than common alternatives such as an overall historical average of LGD or a table of average LGDs. LossCalc’s performance is superior in terms of both out-of-sample out-of-time prediction error and correlation of the predictions with actual recovery experience. The model was also better at identifying low recoveries than historical average methods and had fewer large errors.

Since risk management applications place particular demand upon the estimation of parameter uncertainty, we have developed a conditional confidence interval prediction approach that results in narrower confidence intervals than alternative approaches. In validation testing, these intervals also more accurately represented the true variability of actual recoveries. Combining the results of Moody’s two models, RiskCalc for default probabilities and LossCalc for recovery rates, is natural. With this combination, a risk manager can estimate the expected credit losses of an instrument, given knowledge of the exposure amount. This is a much more complete portrayal of credit risk than probability of default alone.

Estimation of the average (mean expected) losses due to credit is commonly used to:

1. set reserve requirements for doubtful accounts;
2. establish minimum pricing levels at which new credit exposures to an obligor may be undertaken;
3. price credit risky instruments such as corporate bonds or credit default swaps; and
4. calculate risk-adjusted performance measures such as RAROC.

LossCalc’s estimate of the downside confidence bound of LGD (an 80% two-tailed confidence interval) gives greater meaning, consistency, and guidance to stressing recovery rate estimates and for provisioning.

LossCalc represents a robust and validated model of United States LGD for the debt types it covers. We believe that this is a productive step forward in answering the call for rigor that the BIS has outlined in the recently proposed Basel Capital Accord.
APPENDIX A: BETA TRANSFORMATION TO NORMALIZE LOSS DATA

To create an approximately normally distributed dependent variable from the raw observations of recovery, we first confirmed that defaulted debt valuations were approximately Beta distributed. There is no theoretical reason that this is the "correct" shape of the defaulted debt prices, but previous studies have concluded that its characteristics make the Beta a reasonable description of the empirical shape.

Beta-distributions are described in this case by an upper and lower bound and by two shape parameters, $\alpha$ and $\beta$. Most commonly, it is naturally bounded between zero and one; its mean can be any value strictly within its range. The conversion of the Beta distributed recovery values to a more normally distribution dependent variable is explicitly defined as follows:

$$Dependent\ Variable = Y_i = N^{-1}[Betadist(RecoverRt, \alpha_d, \beta_d, Min, Max)]$$

where

- $RecoverRt = \min(Max - \varepsilon, \text{observed\ recovery\ rate})$ where $\varepsilon = \text{some\ small\ value}$
- $\alpha_d = \text{The\ Beta\ Distribution's\ center\ parameter}$
- $\beta_d = \text{The\ Beta\ Distribution's\ shape\ parameter}$
- $Min = \text{Set\ to\ zero\ for\ all\ cases}$
- $Max_d = \text{Set\ to\ 1.1\ for\ bonds,\ but\ otherwise\ is\ 1.0}$
- $d = \{\text{loans, bonds, preferred\ stock}\}$

The sub-notation "d" is only used to emphasize that LossCalc fits each debt-type to its own distribution.

Thus, much of the distributions of our three disparate separate asset classes can be captured by specifying only two shape parameter values: the $\alpha$ and the $\beta$ of each Beta-distribution. It is also possible, through algebraic manipulation, to specify the Beta-distribution that simply matches the mean and standard deviation, which are functions of the shape and boundary parameters.

Mathematically, a Beta-distribution is a function of Gamma distributions. With the lower bound set to zero, the distribution can be described as follows:

$$Beta(x, \alpha, \beta, Min = 0, Max) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} \left( \frac{x}{Max} \right)^{\alpha - 1} \left( 1 - \frac{x}{Max} \right)^{\beta - 1} \left( \frac{1}{Max} \right)$$

The shape parameters can be derived in a variety of ways. For example, the following give them in terms of population mean and standard deviation.

$$\alpha = \frac{\mu}{\mu_{\max}} \left( \frac{\mu}{Max\sigma^2} - 1 \right) \quad \text{and} \quad \beta = \alpha \left( \frac{Max}{\mu} - 1 \right)$$

Conversely, given Beta-distribution parameters, it is straightforward to calculate the mean and standard deviation.

$$\mu = \frac{\alpha}{\alpha + \beta} \text{Max} \quad \text{and} \quad \sigma = \sqrt{\frac{\alpha\beta}{(\alpha + \beta)^2 + (1 + \alpha + \beta^2)\text{Max}}}$$
APPENDIX B: AN OVERVIEW OF THE VALIDATION APPROACH

To validate the performance of LossCalc, we have used the approach adopted and refined by Moody’s and used to validate Moody’s quantitative default prediction models (RiskCalc). The approach, termed walk forward validation, is a robust means for ensuring that:

- models have not been “over-fit” to the data;
- future performance can be well understood; and
- the modeling approach, as well as any individual model produced by it, is robust through time and credit cycles.

We give only a brief overview of the methodology here; a fuller description is detailed in Sobehart, Keenan, & Stein [2000].

B.1. Controlling For "Over Fitting" Risk: Walk-forward Testing

In order to avoid embedding unwanted sample dependency, we have found it useful to develop and validate models using some type of out-of-sample, out-of-universe and out-of-time testing approach on panel or cross-sectional datasets. However, such an approach can generate false impressions about reliability of a model if done incorrectly. "Hold out" testing can sometimes miss important model problems, particularly when processes vary over time, as credit risk does. Dhar & Stein [1997] suggest a framework for framing these issues as well as providing a more detailed discussion and some examples from finance.

Our testing approach is designed to test models in a realistic setting, emulating closely the manner in which the models would be used in practice. The procedure we describe is often referred to in the trading model literature as "walk-forward" testing.

The walk-forward procedure works as follows:

1. Select a year, for example, 1991.
2. Fit the model using all the data available on or before the selected year.
3. Once the model’s form and parameters are established for the selected period, generate the model outputs for all of the firms available during the following year (in this example 1992). Note that these are out-of-time and generally out-of-sample.
4. Save the prediction as part of a result set.
5. Now move the window up one year (e.g.: to 1992) so that all the data through that year can be used for fitting and the data for the following year can be used for testing.
6. Repeat steps (2) to (5) adding the new predictions to the result set.

Collecting all the out-of-sample and out-of-time model predictions produces a set of model performances. This validation result set can then be used to analyze the performance of the model in more detail.

Note that this approach simulates, as closely as possible given the limitations of the data, the process by which the model will actually be used in practice. Each year, the model is refit and used to predict recoveries one year hence. The walk-forward validation process is outlined in Figure 14.

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21. Much of what follows was adapted from Sobehart, Keenan, & Stein [2000].
22. A panel dataset contains observations over time on many individuals. A cross sectional dataset contains one observation on many individuals.
23. See, for example, Mensah [1984].
Note that this approach has two significant benefits. First, it allows us to get a realistic view of how a particular model would perform over time. Second, it allows us to leverage to a higher degree the availability of data for validating models. However, before turning to model performance evaluation, it is important to note that the result set is itself a sub-sample of the population. Therefore, it might possibly yield spurious model performance differences based solely on data anomalies. A common approach to addressing this issue, and one used extensively in our research, is to use one of a variety of resampling techniques to leverage the available data and reduce the dependency on the particular sample at hand.24

Unless otherwise noted, all results presented in this study are from out-of-sample-out-of-time walk-forward testing.

B.2. Resampling

It is important to consider that because of the sparseness of defaults (and thus recoveries) in most credit data; accuracy statistics may sometimes yield spurious model performance differences based only on data anomalies. To understand these problems we combine the above performance measures with resampling techniques to leverage the available data and reduce the dependency on the particular sample at hand. A typical resampling technique proceeds as follows. From the result set, a sub-sample is selected at random. The performance measure of interest (e.g., mean squared error of the predictions) is calculated for this sub-sample and recorded. Another sub-sample is then drawn, and the process is repeated. This continues for many repetitions until a distribution of the performance measure is established. The distribution of these results is then used to calculate the variability of the reported performance measure.

Resampling approaches provide an estimate of the variability around the actual reported model performance. An example is the standard error. This estimate can then be used to assess the significance of observed differences in model performance.

24. For data bootstrap, see Efron & Tibshirani [1993], for randomization tests and cross-validation, see Sprent [1998].
GLOSSARY OF TERMS

Absolute Priority Rule:
Strictly interpreted, a junior class or creditor cannot receive any value in bankruptcy resolution if the more senior classes have not yet been fully satisfied. This rule guides allocations among creditor classes concerning a plan of reorganization, but is rarely strictly applied. Commonly, the bankruptcy court will give some amount of consideration to lower class creditors and/or to preferred and common stockholders in order to circumvent objections, delays, and other litigation.

Debt-type or Instrument Type:
The form of the credit obligation, (e.g., bank loan, public bond, preferred stock).

Expected Recovery Given Default (ERGD):
Recovery, in this context, is the compliment of loss. See, "Recovery Rate."

Loss Given Default (LGD):
Typically stated as a percent of the debt’s par value, it is one minus the recovery rate. This is the terminology used by the BIS. See "Recovery Rate."

Loss in the Event of Default (LIED):
See "Loss Given Default."

Normalization:
Variables can be characterized by their central tendency (average), volatility (standard deviation), skewness (tendency to bunch up towards one end of its range), etc. These measures help describe the variable’s shape or distribution. For many observations in nature, variables have a bell-shaped (a.k.a., Normal or Gaussian) distribution. If a variable is not normally distributed, a transformation can typically be devised that will convert it to be Normal. An inverse of this transformation would reverse the effect. This sort of transformation is termed Normalization.

Priority of Claims:
A plan must classify claims into "substantially similar" groups known as classes. Classification of claims reflects differences in the rights of creditors that call for a difference in treatment. Not all claims that are substantialy similar need be placed in the same class, but those that are placed in the same class must be alike. Unsecured creditors are frequently classified together, whereas each secured claim is generally classified separately. Claims within each class must be treated equally, and a plan must not unfairly discriminate between creditors (whether or not classified together) of equal priority.

Recovery Rate:
The value that a creditor would receive in satisfaction of the claims on a defaulted credit. LossCalc states this as a percentage of the debt’s par value, which is the most common practice. An alternative definition, which is common in the reduced form models, is to state recovery as a percentage of market value. This definition is more tractable, but is not well aligned with creditor’s true claims in default.

Seniority Class:
We use this term to include seniority grades across all debt-types. In a bankruptcy proceeding, all credit obligations of a firm are assigned to a seniority class and the classes are ranked by their seniority standing. In an idealized example, all claims in the highest seniority class would be satisfied before claims below them. Applying the Absolute Priority Rule in a kind of "stair-step" or "waterfall" does this.

Seniority Grade:
Within an instrument type (e.g., public bonds) there is often distinction in seniority such as between secured vs. unsecured or senior vs. subordinated.

25. See Gurdip, Madan & Zhang [2001], Jarrow [2001] and Unal, Madan & Guntay [2000].
BIBLIOGRAPHY


